



# **An Atlas of Internal Solitary-like Waves and their Properties**

**Christopher R. Jackson  
John R. Apel**

**May 2002**

Prepared under contract with  
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Code 322PO  
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Global Ocean Associates  
14605 Carrolton Rd.  
Rockville, MD 20853

## **On the Cover**

Photo of the Strait of Gibraltar taken from the U.S. Space Shuttle (STS-41G) on October 11, 1984, at 12:21:48 GMT. Two packets of solitons are seen to the east; older packets are visible along Spanish and Moroccan coasts. Original Image (S17-34-81) courtesy of Earth Sciences and Image Analysis Laboratory, NASA Johnson Space Center (<http://eol.jsc.nasa.gov>)



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This Atlas is dedicated to Dr. John R. Apel who conceived of creating it. John was a dedicated scientist, a respected colleague and a good friend to many in the oceanographic community.

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